```
COS 226 Fall 2O12 Quiz 1 30 pts.; }30\mathrm{ minutes; }4\mathrm{ questions; }4\mathrm{ pages. 2012-09-20 2:00 p.m.
(c)2012 Sudarshan S. Chawathe
```


## Name:

$\qquad$

1. (1 pt.)

- Read all material carefully.
- You may refer to your books, papers, and notes during this test.
- No computer or network access of any kind is allowed (or needed).
- Write, and draw, carefully. Ambiguous or cryptic answers receive zero credit.
- Use the conventions used in class and the textbook for notation, algorithmic options, etc.

Write your name in the space provided above.
2. ( 9 pts.) Depict the sequence of AVL-tree states resulting from the insertion of the following keys, in the order presented, into an initially empty tree. You must depict the state of the tree after each insertion, clearly marking and identifying (single, double) any rotations used.

$$
16,2,68,47,47,65,76,20,83,17
$$

[additional space for answering the earlier question]
3. (10 pts.) Repeat Question 2 for red-black trees. Follow the graphical conventions used in class: round nodes for red and boxed nodes for black.
4. (10 pts.) For each value of $n=2,3,4$, depict all possible red-black trees containing the $n$ keys $1,2, \ldots, n$. Justify your answer briefly, explaining why the trees you depict are the only ones possible.

