COS 451 Spring 2013 Class Exercise 14 2 questions; 2 pgs. 2013-03-26

Today HW05 due. The class P; CYK algorithm. §7.2.
Next class The class NP, and NP-completeness. $\S \S 7.3-4$. Quiz next week.

1. List the members of your group below. Underline your name.
2. Trace Euclid's algorithm to compute the GCD of 3838 and 19302.
3. Prove or disprove each: The class P is closed under
(a) complement.
(b) union.
(c) concatenation.
4. The operation of the algorithm of Theorem 7.16 (CYK) on the following grammar with and string 000\#111 is depicted by the table on the right below.

|  | $i \backslash j$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $S_{0} \rightarrow \# \mid N_{2} N_{0}$ | 1 | $\left\{N_{2}\right\}$ | $\emptyset$ | $\emptyset$ | $\emptyset$ | $\emptyset$ | $\emptyset$ | $\left\{S_{0}\right\}$ |
| $\begin{aligned} S_{0} & \rightarrow \# \mid N_{2} N_{0} \\ B & \rightarrow \#\end{aligned}$ | 2 |  | $\left\{N_{2}\right\}$ | $\emptyset$ | $\emptyset$ | $\emptyset$ | $\left\{S_{0}\right\}$ | $\left\{N_{0}\right\}$ |
| $\begin{aligned} B & \rightarrow \\ N_{0} & \rightarrow S_{0} N_{4}\end{aligned}$ | 3 |  |  | $\left\{N_{2}\right\}$ | $\emptyset$ | $\left\{S_{0}\right\}$ | $\left\{N_{0}\right\}$ | $\emptyset$ |
| $N_{0} \rightarrow S_{0} N_{4}$ $N_{2} \rightarrow 0$ | 4 |  |  |  | $\left\{S_{0}, B\right\}$ | $\left\{N_{0}\right\}$ | $\emptyset$ | $\emptyset$ |
| $N_{2} \rightarrow 0$ $N_{4} \rightarrow 1$ | 5 |  |  |  |  | $\left\{N_{4}\right\}$ | $\emptyset$ | $\emptyset$ |
| $N_{4} \rightarrow$ | 6 |  |  |  |  |  | $\left\{N_{4}\right\}$ | $\emptyset$ |
|  | 7 |  |  |  |  |  |  | $\left\{N_{4}\right\}$ |

Depict a similar table for the operation of the algorithm on string $a+a *(a+a)$ for the grammar:

```
S0 -> N19 NO | S0 N1 | a | term N2
NO -> SO N10
N1 -> N11 term
factor -> N19 NO | a
term -> N19 NO | a | term N2
```

```
N10 -> )
N11 -> +
N12 -> *
N19 -> (
N2 -> N12 factor
```

