COS 451 Spring 2013 <u>Midterm Exam 2</u> 60 minutes; 60 pts.; 5 questions; 7 pgs.

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Name:

- 1. (1 pt.)
  - Read all material carefully.
  - You may refer to your books, papers, and notes during this test.
  - No computer or network access of any kind is allowed (or needed).
  - Write, and draw, carefully. Ambiguous or cryptic answers receive zero credit.
  - Use textbook and classroom conventions for notation, algorithmic options, etc.
  - Ask for clarifications on the above if needed.

Write your name in the space provided above.

2. (14 pts.) Convert the following grammar to Chomsky normal form. Upper-case letters denote variables and lower-case letters denote terminals. *Show enough intermediate results and include brief explanations* to make it clear that the method described in the textbook is being followed.

$$\begin{array}{rrrr} A & \rightarrow & aa \mid ABA \\ B & \rightarrow & b \mid bAbA \mid \epsilon \end{array}$$

[additional space for answering the earlier question]

3. (15 pts.) Using the tabular representation used in class, depict the operation of the CYK algorithm on the input string aabaabaaaa and the final (Chomsky normal form) grammar of Question 2.

- 4. (15 pts.)
  - (a) Reduce the following SAT instance to a SUBSET-SUM using the textbook's method.
  - (b) Depict corresponding solutions to the instances, or explain why none exist.

 $(x \lor y \lor z) \land (\bar{x} \lor \bar{y} \lor z) \land (x \lor \bar{y} \lor \bar{z}) \land (\bar{x} \lor y \lor \bar{z}) \land (x \lor \bar{y} \lor z)$ 

[additional space for answering the earlier question]

5. (15 pts.) Repeat Question 4, but reduce the SAT instance to an instance of CLIQUE (instead of SUBSET-SUM).

[additional space for answering the earlier question]