© 2013 Sudarshan S. Chawathe

Today's topic: equivalence classes, union-find data structures; §§ 24.{1-4} Next class: Synthesis: Kruskal's algorithm (graphs, union-find, paring heap).

- 1. List the members of your group below. Underline your name.
- 2. Provide an illustrative example of an equivalence relation R by specifying the base set S of elements and the pairs  $x, y \in S$  for which xRy is true. Do not reuse the examples in the textbook.

Repeat for relations  $R_1$ ,  $R_2$ , and  $R_3$  which are not equivalence relations because they violate the requirements of reflexivity, symmetry, and transitivity, respectively (with each  $R_i$  satisfying the other two requirements).

3. Depict the tree resulting from find(7) applied to the tree of Figure 24.17 when path compression is in use. How many nodes get their parents changed?

4. Starting with each of the items 0, 1, 2, ..., 15 in a singleton set by itself, provide an explicit sequence (as short as possible) of operations that yields the tree of Figure 24.17 in the textbook when using the union-by-size smart-union algorithm. Depict the forest before and after the *last two* operations.

5. Consider the effect of *path compression* on the structure Question 4. Suppose we are permitted to augment the sequence of operations of Question 4 by introducing two *find* operations of our choice into the sequence, at positions of also of our choice. If our goal is to minimize the height of the resulting structure, what are the best choices for the find operations and their positions? Explain.