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COS 451 Spring 2014 Class Exercise 13 4 questions; 2 pgs.

Today The class P; CYK algorithm. §7.2.
Next class The class NP, and NP-completeness. §§7.3-4.
1. List the members of your group below. Underline your name.
2. Trace Euclid's algorithm to compute the GCD of 3838 and 19302.
3. Prove or disprove each: The class P is closed under
(a) complement.
(b) union.
(c) concatenation.
4. The operation of the algorithm of Theorem 7.16 (CYK) on the following grammar with and string 000\#111 is depicted by the table on the right below.
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline & \(i \backslash j\) & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\
\hline \(\rightarrow \quad \# \mid N_{2} N_{0}\) & 1 & \(\left\{N_{2}\right\}\) & & \(\emptyset\) & \(\emptyset\) & \(\emptyset\) & \(\emptyset\) & \(\left\{S_{0}\right\}\) \\
\hline \(S_{0} \rightarrow\)
\(B \rightarrow \#\) & 2 & & \(\left\{N_{2}\right\}\) & \(\emptyset\) & \(\emptyset\) & \(\emptyset\) & \(\left\{S_{0}\right\}\) & \(\left\{N_{0}\right\}\) \\
\hline \(N_{0} \rightarrow \rightarrow S_{0} N_{4}\) & 3 & & & \(\left\{N_{2}\right\}\) & \(\emptyset\) & \(\left\{S_{0}\right\}\) & \(\left\{N_{0}\right\}\) & \(\emptyset\) \\
\hline \(N_{0} \rightarrow S_{0} N_{4}\)
\(N_{2} \rightarrow 0\) & 4 & & & & \(\left\{S_{0}, B\right\}\) & \(\left\{N_{0}\right\}\) & \(\emptyset\) & \(\emptyset\) \\
\hline \(N_{4} \rightarrow 1\) & 5 & & & & & \(\left\{N_{4}\right\}\) & \(\emptyset\) & \(\emptyset\) \\
\hline \(\mathrm{N}_{4} \rightarrow\) & 6 & & & & & & \(\left\{N_{4}\right\}\) & \(\emptyset\) \\
\hline & 7 & & & & & & & \(\left\{N_{4}\right\}\) \\
\hline
\end{tabular}

Depict a similar table for the operation of the algorithm on string \(a+a *(a+a)\) and grammar:
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S0 -> N19 N0 | SO N1 | a | term N2
NO -> SO N10
N1 -> N11 term
factor -> N19 NO | a
term -> N19 NO | a | term N2

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N10 -> )
N11 -> +
N12 -> *
N19 -> (
N2 -> N12 factor

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