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COS 454/554 Spring 2021 Class Exercise 5 4 questions; 2 pgs. 2021-04-09
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Today Divide and Conquer; recurrences. $\S \S 4 .\{1,2,3\}$.
Next class Elementary Graph Algorithms. §§ 22.*.

1. Write your name below.
2. Trace the execution of the Find-Max-Crossing-Subarray algorithm on the array A depicted below, with the arguments low, mid, and high equal to 1,5 , and 10 , respectively.

A[i]:

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 88 | 19 | 9 | -66 | -2 | 116 | -56 | -12 | 87 | 101 |

List the values of sum and left-sum after each iteration of the first for-loop of the algorithm. Similarly, list the values of sum and right-sum after each iteration of the second for-loop.
3. Depict the recursion tree that outlines the recursive calls made by the Find-MaximumSUbARRAY algorithm when invoked on the array of Question 2 (repeated below), with low and high equal to 1 and 10 , respectively. The nodes of the tree should be labeled with the function invoked (Find-Maximum-Subarray or Find-Max-CrossingSUBARRAY and the edges should connect each function's node to the node of its invoker.

A[i]:

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 88 | 19 | 9 | -66 | -2 | 116 | -56 | -12 | 87 | 101 |

4. Provide an asymptotic solution (big $\Theta$ ) for the following recurrence. Explain briefly.

$$
S(n)=n^{2}-n+S(n-2)
$$

