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COS 454/554 Fall 2O23 Quiz 2 45 minutes; 45 pts.; }9\mathrm{ questions; }6\mathrm{ pgs. 2023-11-03 9:05 a.m.
@ 2023 Sudarshan S. Chawathe
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Name: $\qquad$

1. (1 pt.)

- Read all material carefully.
- If in doubt whether something is allowed, ask, don't assume.
- You may refer to your books, papers, and notes during this test.
- E-books may be used subject to the restrictions noted in class.
- Computers (including smart phones, tablets, etc.) are not permitted, except when used strictly as e-books or for viewing ones own notes.
- Calculators are not required but are permitted.
- Network access of any kind (cell, voice, text, data, ...) is not permitted.
- Write, and draw, carefully. Ambiguous or cryptic answers receive zero credit.
- Use class and textbook conventions for notation, algorithmic options, etc.
- Do not attach or remove any pages.

Write your name in the space provided above.
Do not write anything else on this page.

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WAIT UNTIL INSTRUCTED TO CONTINUE TO REMAINING QUESTIONS.
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(Do not view any other pages.)

Do not write on this page.
(It is for use in grading only.)

| Q Full | Score |
| ---: | ---: | ---: |
| 1 | 1 |
| 2 | 5 |
| 3 | 5 |
| 4 | 5 |
| 5 | 5 |
| 6 | 5 |
| 7 | 5 |
| 8 | 5 |
| 9 | 9 |
| total | 45 |

2. ( 5 pts. ) Consider the following binary-string code, following the conventions used in class: $(a, b, c)=(01,00, x)$. List all possible values for $x$ that result in a prefix-free code. Explain your answer.
3. (5 pts.) Repeat Question 2 but with prefix-free code replaced by fixed-length code
4. (5 pts.) Following the conventions used in class and the textbook, depict the final tree produced by Huffman's Algorithm on the following input. (You do not need to depict intermediate trees, but doing so will permit better partial credit in case of errors.)

| character: | C | D | F | T | V | W |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| frequency: | 39 | 17 | 22 | 30 | 6 | 5 |

5. (5 pts.) Describe as precisely as you can, in plain English (or, if you prefer, pseudocode), the standard greedy algorithm for the (coin) change-making problem as discussed in class. Be sure to clearly indicate the input and output in addition to the program logic.
6. ( 5 pts .) Is the algorithm of Question 5 guaranteed to provide an optimal solution? Explain your answer as precisely as you can, providing either proof of or counterexample for the claim of optimality.
7. (5 pts.) Using the conventions described in class, depict the adjacency lists representation of the following graph.

8. (5 pts.) Repeat Question 7 using adjacency matrix instead of adjacency lists.
9. (9 pts.) Trace the action of the furthest-in-future cache-replacement strategy on the following sequence of block requests, for a cache size of 4 blocks. Break ties by evicting the lower-numbered block. Depict the state of the cache after each request using the format request: resulting-cache-contents. State the number of cache misses.

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